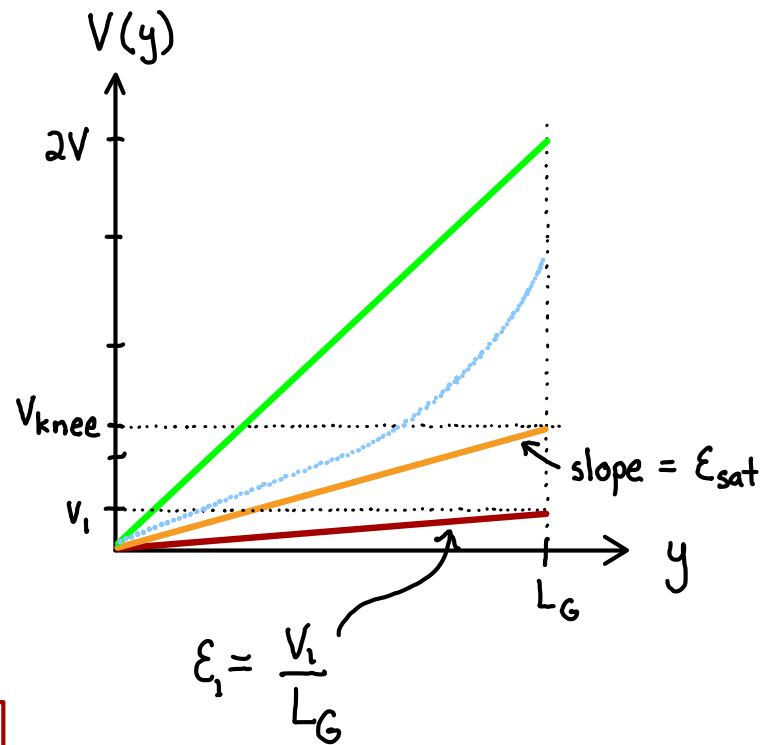
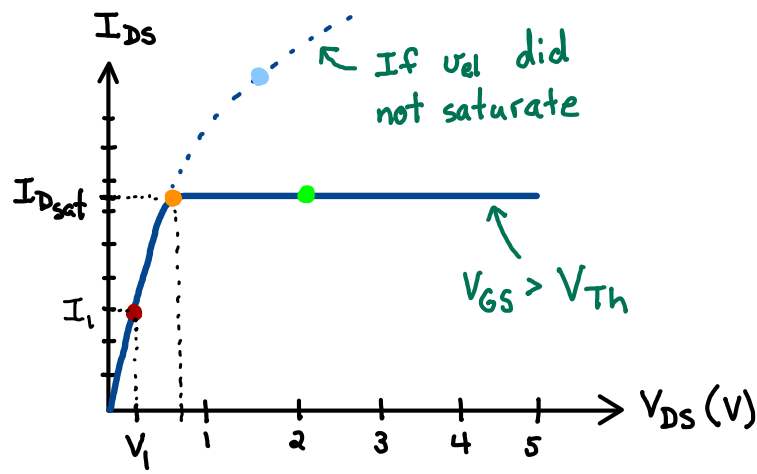


Short Channel MOSFET: ($L_G \lesssim 0.2 \mu m$)

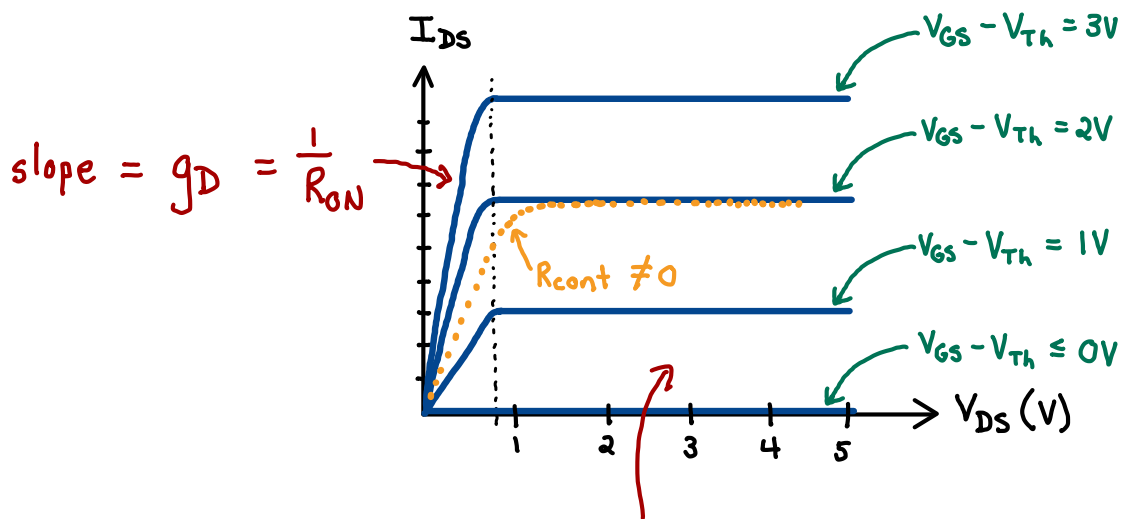


$$V_{knee} = E_{sat} \cdot L_G = \frac{v_{sat}}{\mu_n} L_G$$

$$\begin{aligned} I_1 &= q n_s W_G \cdot v_{el} \\ &= C_{ox} (V_{GS} - V_{TH}) \cdot W_G \cdot \mu_n E_1 \\ &= \frac{W_G}{L_G} \mu_n C_{ox} (V_{GS} - V_{TH}) V_1 \end{aligned}$$

$$\begin{aligned} &\underline{V_{DS} < V_{knee}:} \\ I_{DS} &= \frac{W_G}{L_G} \mu_n C_{ox} (V_{GS} - V_{TH}) V_{DS} \end{aligned}$$

$$\begin{aligned} &\underline{V_{DS} > V_{knee}:} \\ I_{DS} &= I_{DSat} = W_G C_{ox} (V_{GS} - V_{TH}) v_{sat} \end{aligned}$$



Curves evenly spaced in saturation regime ($g_m = \text{const}$)

$$g_m = \left. \frac{\partial I_{DS}}{\partial V_{GS}} \right|_{V_{DS} > V_{knee}} = W G C_{ox} v_{sat}$$

$$R_{ON} = \frac{1}{g_D} = \left[\left. \frac{\partial I_{DS}}{\partial V_{DS}} \right|_{V_{DS} < V_{knee}} \right]^{-1} = \frac{L_G}{W \mu_n C_{ox} (V_{GS} - V_{TH})}$$

If we account for contact resistances ($R_S = R_D = R_{cont}$):

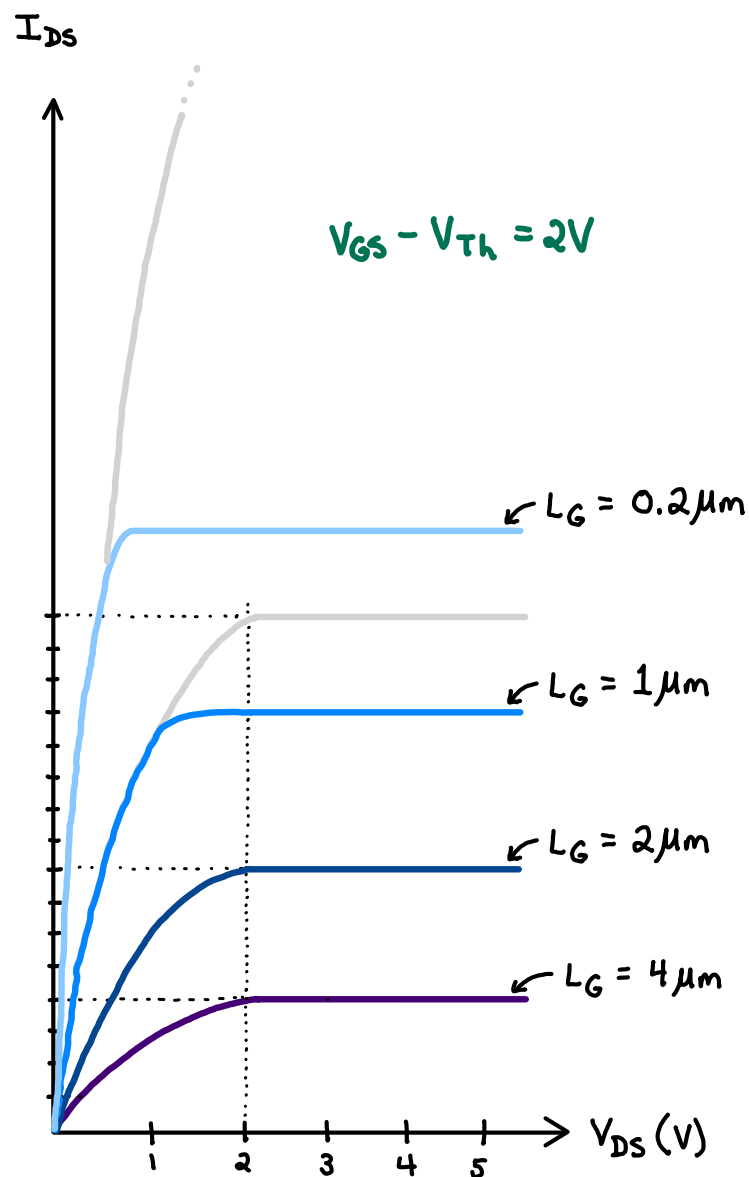
$$R_{ON} = \frac{L_G}{W \mu_n C_{ox} (V_{GS} - V_{TH})} + 2R_{cont}$$

$$\frac{V_{knee}}{I_{Dsat}} = R_{ON} \rightarrow V_{knee} = \frac{v_{sat}}{\mu_n} \cdot L_G + 2W G C_{ox} (V_{GS} - V_{TH}) v_{sat} R_{cont}$$

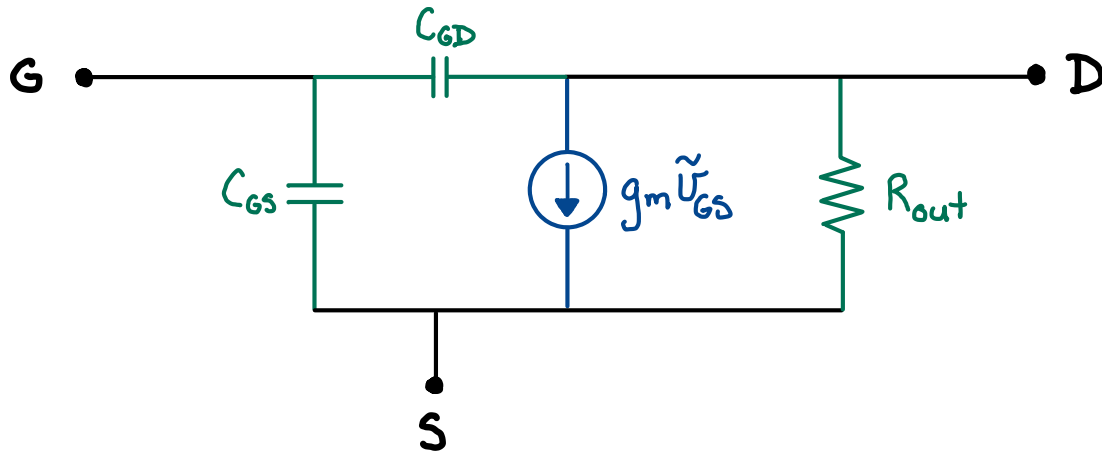
Questions:

1. Referring to the I-V curves on the previous page, how would they differ if L_G was reduced by a factor of 2 (assuming zero contact resistance)?
2. If L_G was reduced by a factor of 2 and t_{ox} was also reduced by a factor of 2 (constant field scaling), how would the I-V characteristics change (assuming no change in V_{th})?

Scaling of MOSFETs



Small-Signal Model



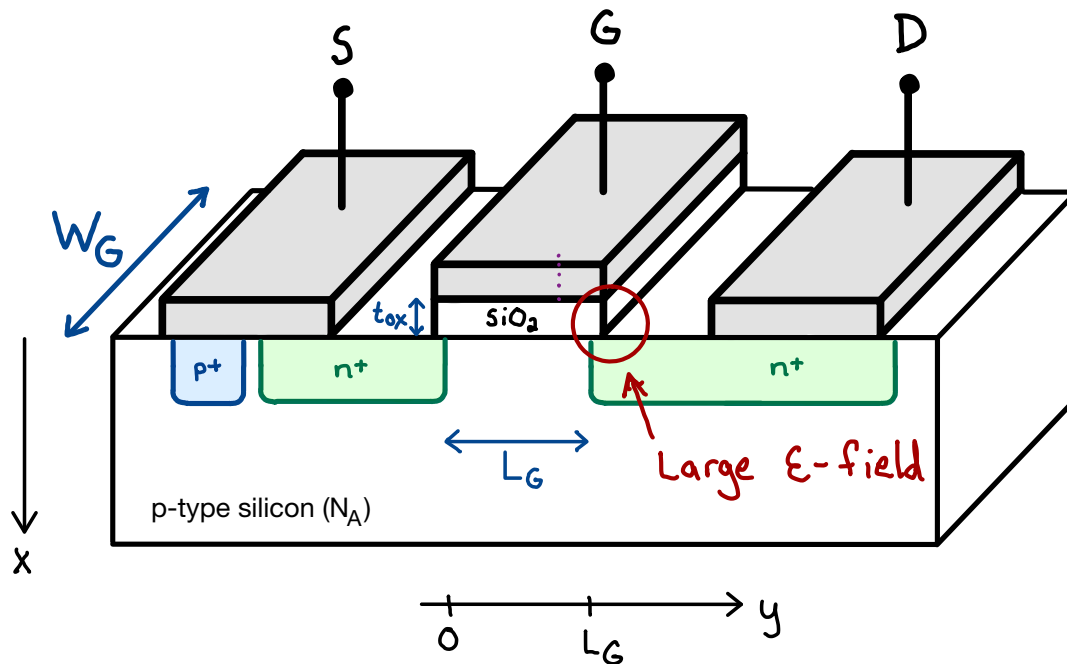
$$f_T = \frac{g_m}{2\pi(C_{GS} + C_{GD})}$$

Short channel:

- g_m does not depend on L_G
- $C_{GS} \sim L_G$ and $C_{GD} \sim L_G$
- If only L_G is varied, $f_T \propto \frac{1}{L_G}$
- Constant field scaling:
 - $g_m \propto \frac{1}{L_G}$
 - $f_T \propto \frac{1}{L_G^2}$

Challenges in scaling of MOSFETs:

1. Small gate lengths
 - EUV lithography technology
2. Thin gate oxides: electron tunneling through gate oxide



$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$$

High-dielectric oxides (High- κ dielectrics):

Al_2O_3	$\epsilon_r = 9.5$
ZrO_2	$\epsilon_r = 20-40$
HfO_2	$\epsilon_r = 20-30$
TiO_2	$\epsilon_r = 80$
Ta_2O_5	$\epsilon_r = 250$