

$$1 \quad \text{MAG} = P_{\text{amp}} / P_{\text{gen, delivered}}$$

$$P_{\text{amp}} = I_{\text{amp}}^2 / G_{\text{ds}}$$

$$I_{\text{amp}} = g_m V_{\text{gs}}$$

$$\frac{V_{\text{gs}}}{V_{\text{gen}}} = \frac{1/j\omega C_{\text{gs}}}{R_i + 1/j\omega C_{\text{gs}}}$$

$$= \frac{1}{R_i j\omega C_{\text{gs}} + 1}$$

$$P_{\text{amp}} = \left( \frac{g_m V_{\text{gen}}}{R_i j\omega C_{\text{gs}} + 1} \right)^2 (R_{\text{os}} \parallel Z_{\text{out}})$$

$$P_{\text{gen, delivered}} = V_{\text{gen}}^2 / 4Z_{\text{gen}}$$

$$\text{MAG} = \frac{g_m^2 V_{\text{gen}}^2}{(R_i j\omega C_{\text{gs}} + 1)^2} \frac{R_{\text{os}} Z_{\text{out}}}{R_{\text{os}} + Z_{\text{out}}}$$

$$\frac{V_{\text{gen}}^2 / 4Z_{\text{gen}}}{V_{\text{gen}}^2 / 4Z_{\text{gen}}}$$

$$= \frac{4g_m^2 Z_{\text{gen}}}{(R_i j\omega C_{\text{gs}} + 1)^2} \left( \frac{R_{\text{os}} Z_{\text{out}}}{R_{\text{os}} + Z_{\text{out}}} \right)$$

Short-circuit current gain

$$I_{\text{out}} / I_{\text{in}} |_{z_L = 0}$$

$$I_{\text{out}} = I_{\text{amp}} (1/G_{\text{ds}})$$

$$= \left( \frac{g_m V_{\text{gen}}}{R_i j\omega C_{\text{gs}} + 1} \right) \frac{1}{G_{\text{ds}}}$$

$$I_{\text{in}} = \frac{V_{\text{gen}}}{Z_{\text{in}}}$$

$$Z_{\text{in}} = Z_{\text{gen}} + R_i + \frac{1}{j\omega C_{\text{gs}}}$$

$$Z_{in} = \frac{V_{gen}}{I_{in}}$$

$$\frac{I_{out}}{I_{in}} = \frac{g_m V_{gen} R_{oe}}{R_i j\omega C_{gs} + 1} \cdot \frac{V_{gen}}{Z_{gen} + R_i + j\omega C_{gs}}$$

$$= \frac{g_m R_{oe} (Z_{gen} + R_i + j\omega C_{gs})}{R_i j\omega C_{gs} + 1}$$

$$b \quad f_T = \frac{g_m}{2\pi C_{gs}} \quad f_{max, fet} = \frac{f_T}{2\sqrt{R_i + R_o + R_g} C_{gs}}$$

$$= \frac{3mS / \mu m \cdot \omega g}{2\pi (0.75 fF / \mu m \cdot \omega g)}$$

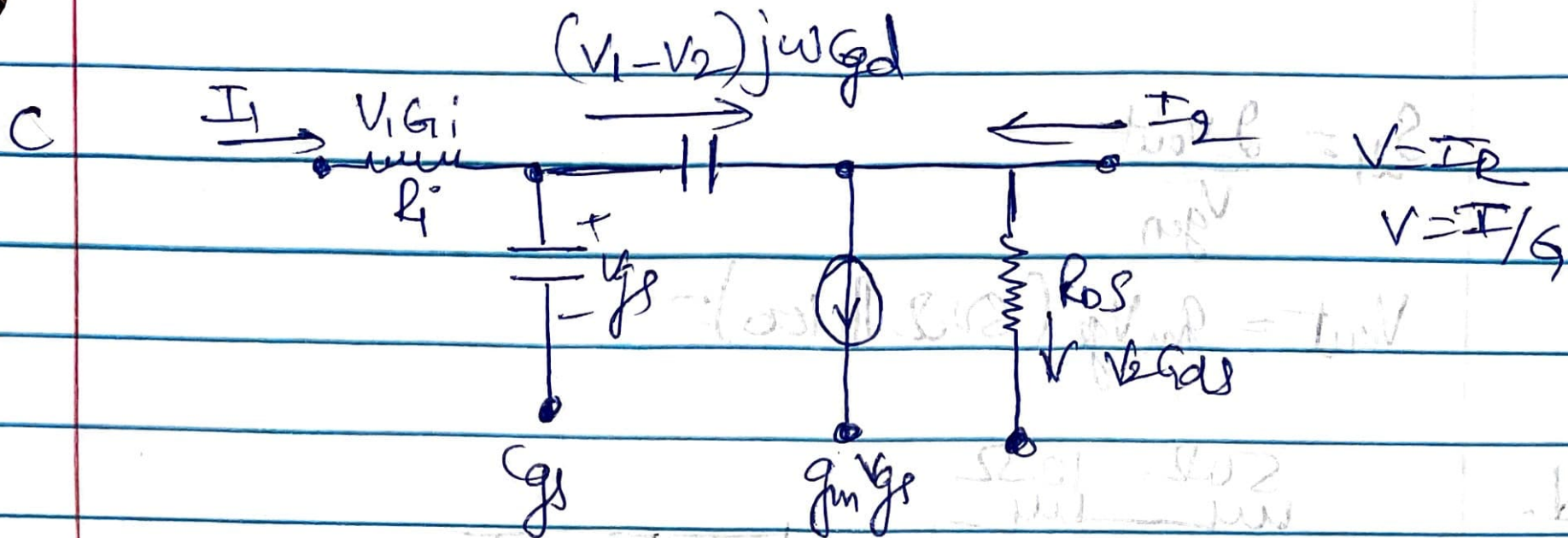
$$= \frac{3mS}{2\pi \cdot 0.75 fF} = 636.9 \text{ GHz}$$

$$f_{max} = \frac{636.9 \text{ GHz}}{2\sqrt{(800)(0.1 \times 10^{-3})}} = 1.42 \text{ THz}$$

with generator and load impedances matched @ 50Ω

$$f_{max/2} = 473.3 \text{ GHz}$$





$$Y_{11} = \frac{1}{R_i} + j\omega C_{gs}$$

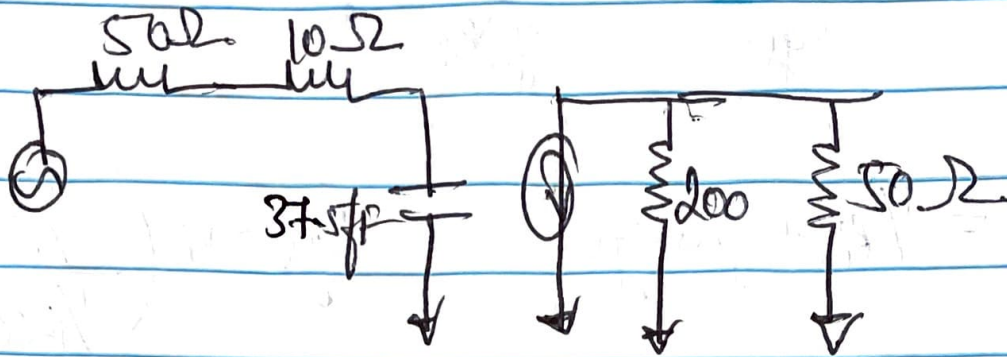
$$V_{gs} = V_i \left( \frac{1/j\omega C_{gs}}{1/j\omega C_{gs} + R_i} \right)$$

$$Y_{21} = \frac{I_2}{I_1} = \frac{g_m \frac{G_i}{G_i + j\omega C_{gs}}}{G_i + j\omega C_{gs}} = \frac{G_i}{G_i + j\omega C_{gs}}$$

$$Y_{22} = G_{ds}$$

$$Y_{12} = 0$$

Ad.



$$S_{11}: Z_{in} = 10 \Omega + 1$$

$$j(2\pi \cdot 100 \times 10^9 \cdot 37.5 \text{ pF})$$

$$= 10 \Omega + 42.44j$$

$$S_{11} = \frac{10 - 42.44j \Omega - 50 \Omega}{10 - 42.44j \Omega + 50 \Omega} = \frac{-40 - 42.44j}{60 - 42.44j}$$

$$\|S_{11}\| = \frac{58.8194}{73.4925} = 0.7935$$

$$S_{12} = 0$$

$$S_{21} = 2 V_{out} / V_{gen}$$

$$V_{out} = g_m V_{gs} (50 \parallel 200)$$

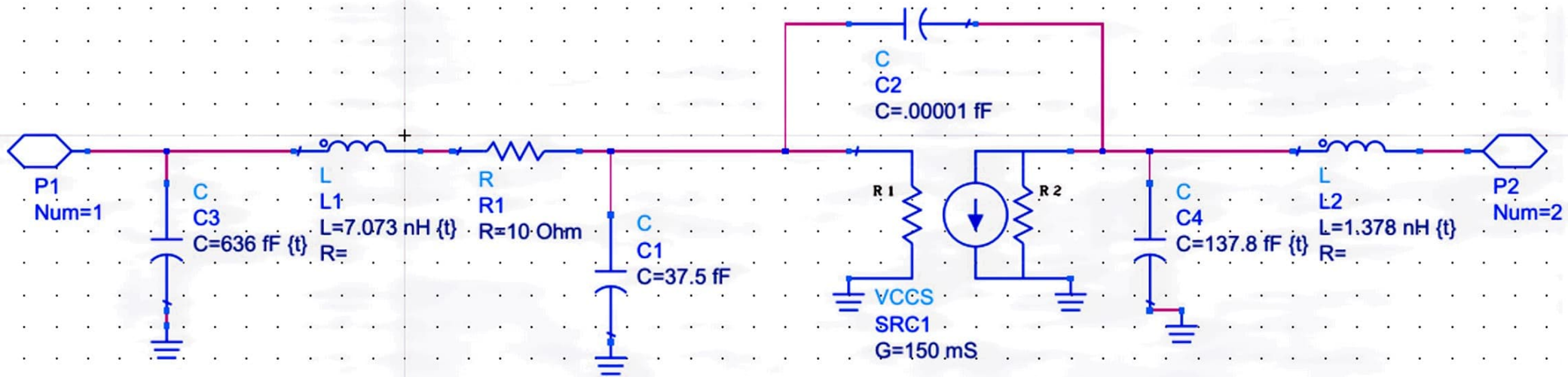
$$= 6 V_{gs} \Rightarrow 2 V_{out} = 12 V_{gs}$$

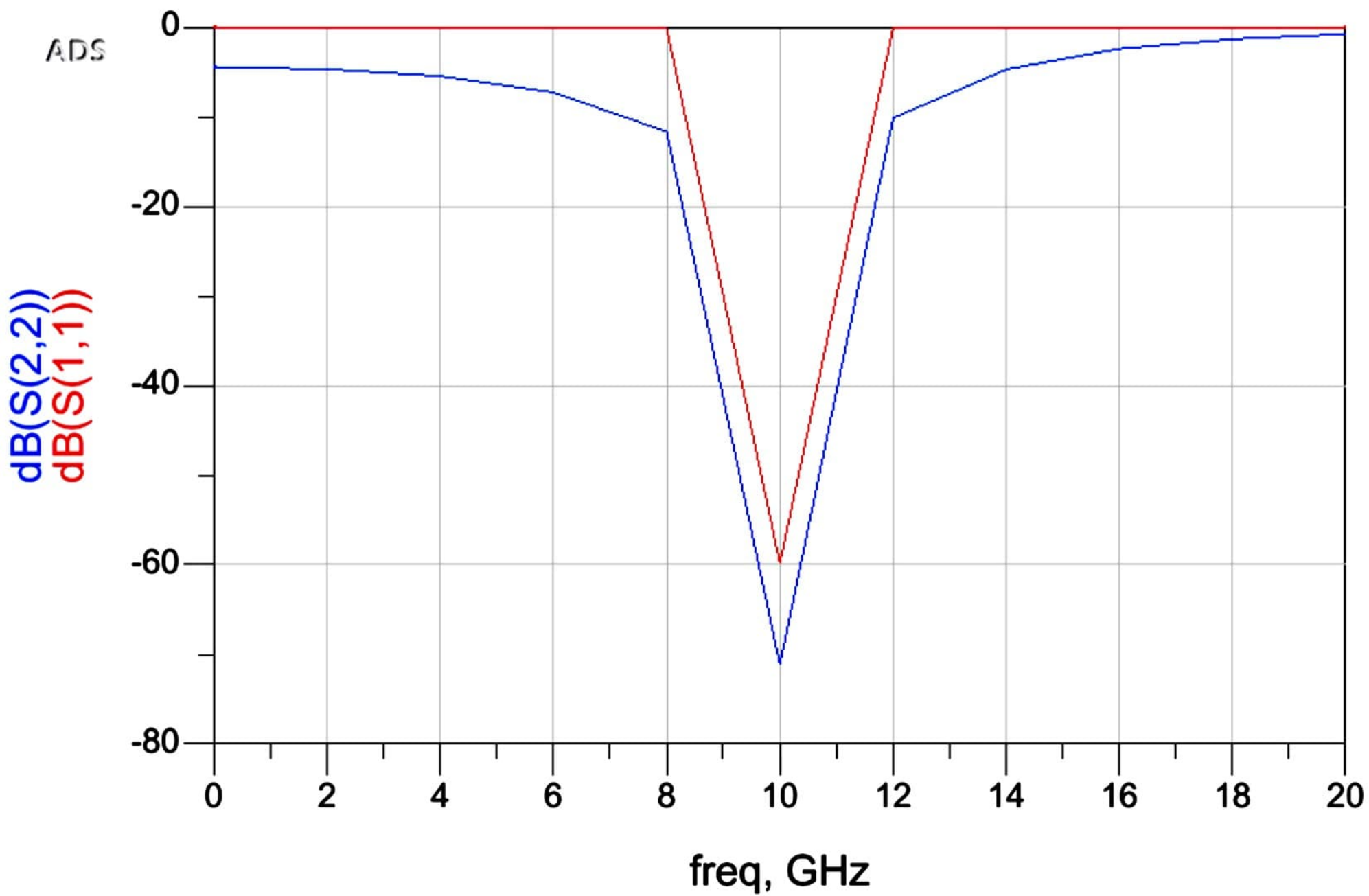
$$S_{21} = \frac{12}{1 + 0.45j} \Rightarrow \|S_{21}\| \approx 48$$

$$V_{gs} = \frac{1}{1 + j\omega C_{gs} 60}$$

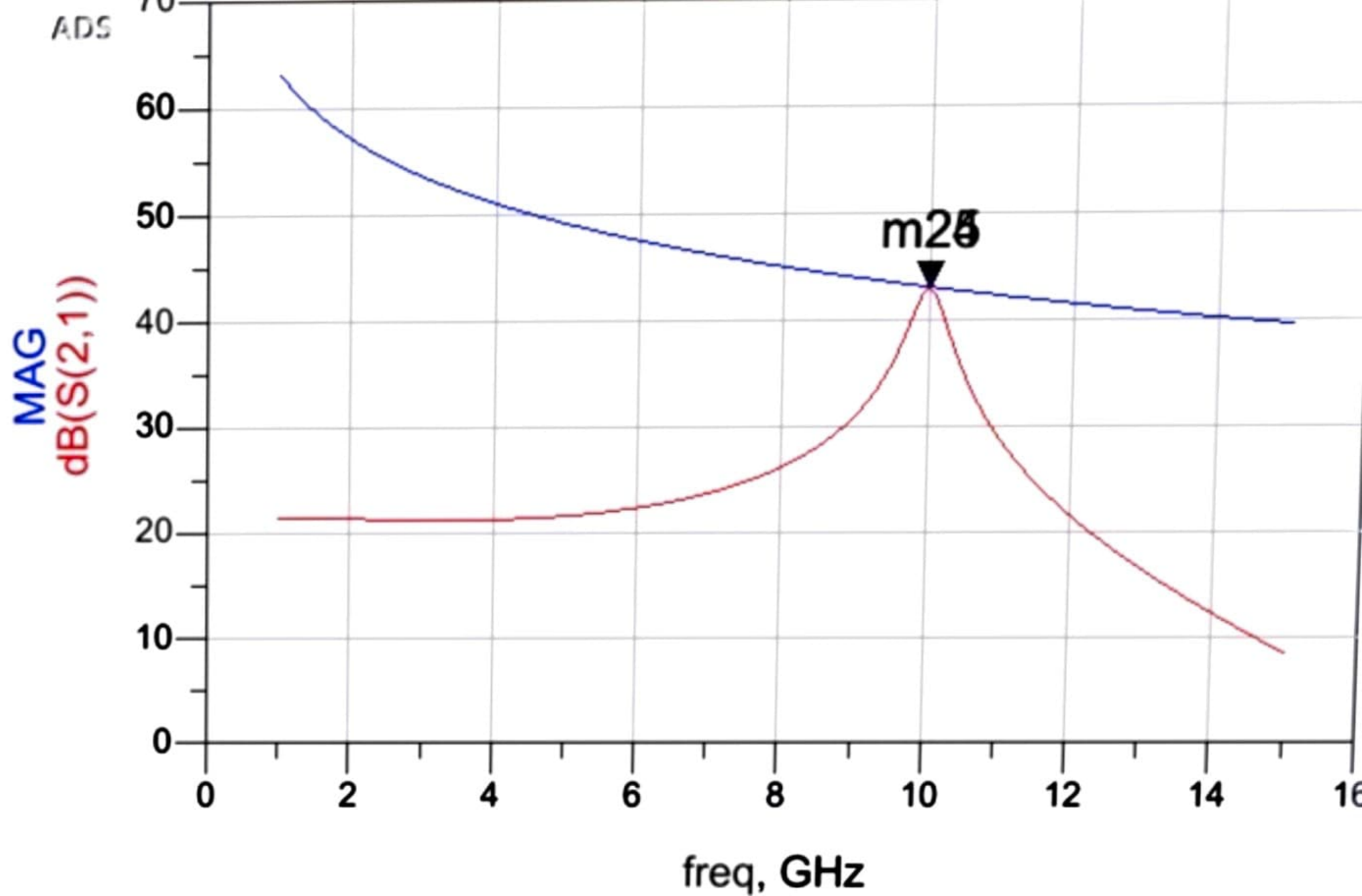
$$S_{22} = \frac{200 - 50}{200 + 50} = 0.6$$

Insertion gain

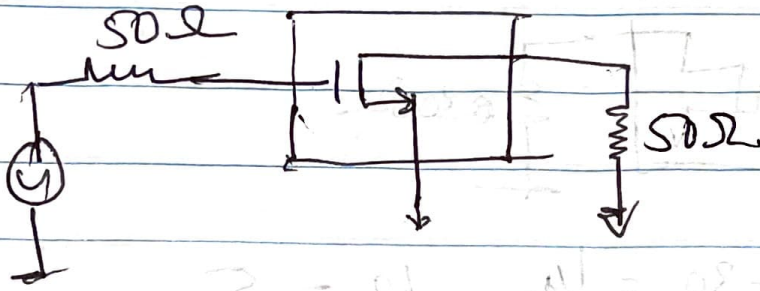








2a.



$S_{12} = 0$  No feedback.

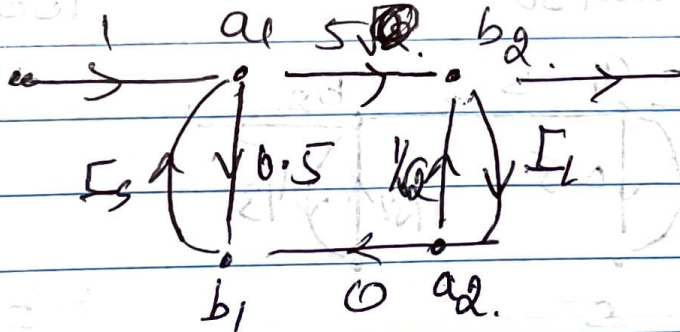
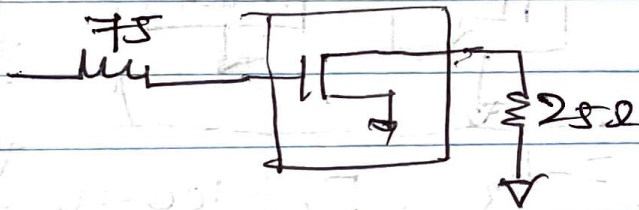
$$\|S_{21}\|^2 = P_{deliv} / P_{av}$$

$50\Omega = Z_0$  network

$$25 = P_{deliv} / 1mW$$

$$P_{deliv} = 250mW$$

2b.



$$\Gamma_s = \frac{75 - 25}{75 + 25} = 1/2$$

$$\frac{b_2}{a_1} = 5$$

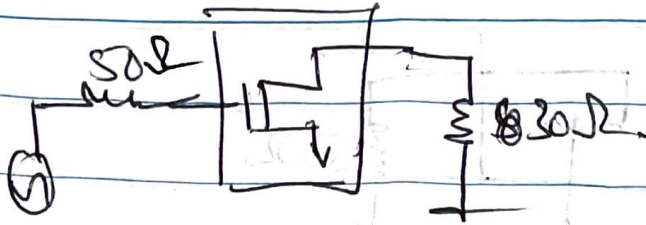
$$\Gamma_L = \frac{25 - 75}{75 + 25} = -1/2$$

$$S_{21,eff} = 4.531$$

$$G_p = \frac{1}{1 - \|\Gamma_{in}\|^2} \cdot \frac{\|S_{21}\|^2 (1 - \|\Gamma_L\|^2)}{\|1 - S_{22}\Gamma_L\|^2} = \frac{4(4.531)^2 \cdot 1.25}{3(1 + 1/2 \cdot 1/2)} = 18.6 \text{ mW} = 18.6 \text{ mW}$$



2c



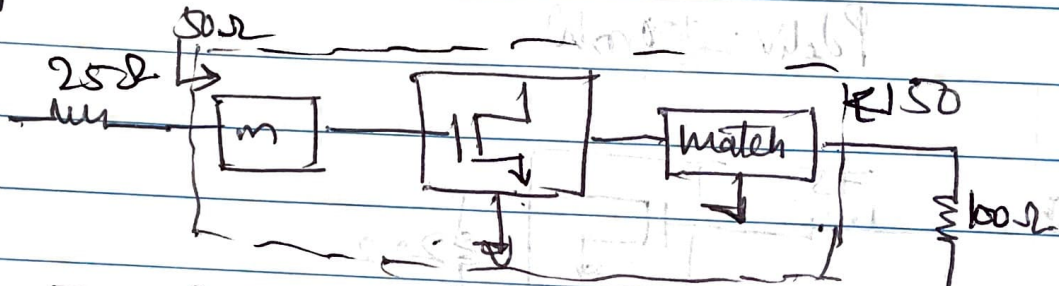
$$\Gamma_s = \frac{50 - 30}{50 + 30} = \frac{1}{4} \quad \frac{b_2}{a_1} = \frac{5}{1 - (0.5(0.25) - 0.25\sqrt{2})}$$

$$\Gamma_L = \frac{30 - 50}{50 + 30} = -\frac{1}{4}$$

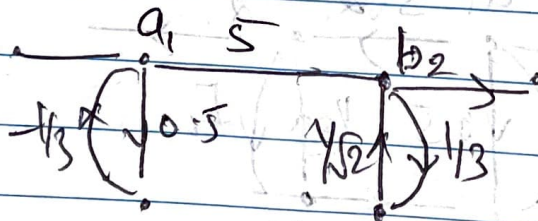
$$S_{2,eff} = 4.754$$

$$P_p = 20.57 \text{ (m)W} = 20.57 \text{ mW}$$

2d.



$$\Gamma_s = \frac{25 - 50}{25 + 50} = -\frac{1}{3} \quad \Gamma_L = \frac{100 - 50}{100 + 50} = \frac{1}{3}$$

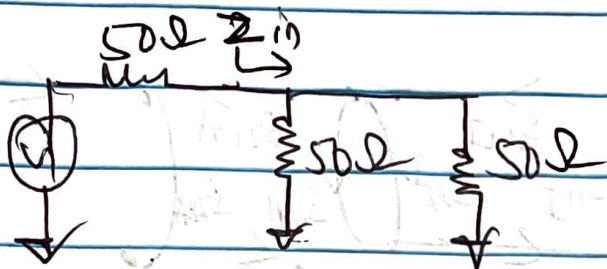


$$\frac{b_2}{a_1} = \frac{5}{1 - (0.5(-1/3) + (\sqrt{2} \cdot 1/3))} = 5.3708$$

$$P_p = \frac{(S_{21})^2}{1 - ||\Gamma_L||^2} \frac{1 - ||\Gamma_s||^2}{1 - \frac{1}{3}(\frac{\sqrt{2}}{3})^2}$$

$$= 43.89 \text{ mW}$$

3a



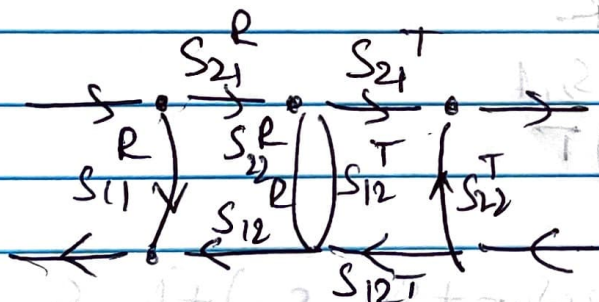
$$S_{11} = \frac{2 \cdot 50\Omega - 50}{2 \cdot 50 + 50} = -1/3$$

$$S_{22} = -1/3$$

$S_{12} = 2/3$  by symmetry

$$S_{21} = 2 \left( \frac{25}{50 + 25} \right) = 2/3$$

3b



$$S_{21} = \frac{S_{21}^R S_{21}^T}{1 - S_{22}^R S_{11}^T} = 6.4004$$

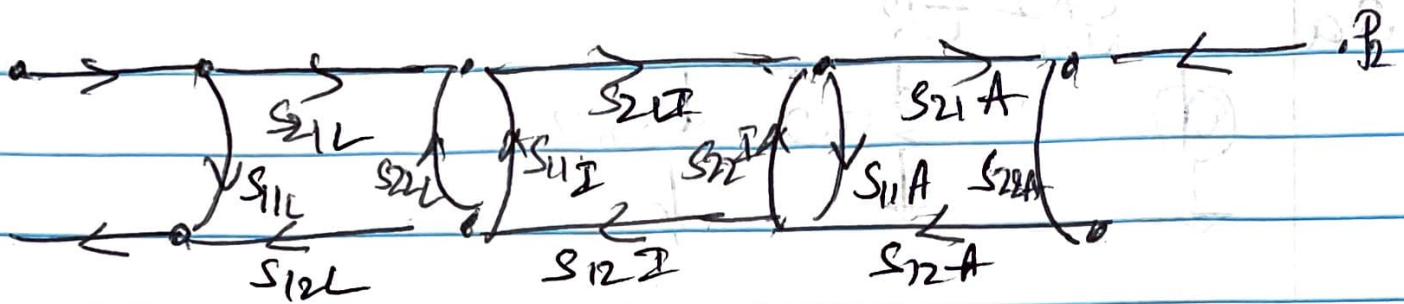
$$S_{11} = \frac{S_{11}^T (1 - S_{22}^R S_{11}^T) + S_{21}^R S_{11}^T S_{12}^R}{1 - S_{22}^R S_{11}^T} = 0.143$$

$$S_{12} = \frac{S_{12}^R S_{12}^T}{1 - S_{22}^R S_{11}^T} = 0.6451$$

$$S_{22} = \frac{S_{22}^T (1 - S_{22}^R S_{11}^T) + S_{12}^T S_{22}^R S_{21}^T}{1 - S_{22}^R S_{11}^T} = -3.1007$$



4.



$$a = 1 - \sum L(i)$$

$$= 1 - (S_{22L} S_{11I} + S_{22I} S_{11A})$$

$$= 1 - 0 = 1$$

$$S_{11} = S_{11L} (1 - S_{22L} S_{11I} + S_{22I} S_{11A}) + S_{21L} S_{11I} S_{12L} (1 - S_{22I} S_{11A})$$

$$+ S_{21L} S_{21I} S_{11A} S_{12I} S_{12L}$$

$$= 0.1 + 10 (0.5) (R) (0.25) (10)$$

$$= 0.1 + 12.5R$$

$$S_{21} = S_{21L} S_{21I} S_{21A}$$

$$= 10 (0.5) T$$

$$= 5T$$

$$S_{22} = S_{22A} (1 - S_{22L} S_{11I} + S_{22I} S_{11A}) + S_{12A} S_{22I} S_{12A}$$

$$(1 - S_{22L} S_{11I} + S_{22I} S_{11A}) + S_{12A} S_{12I} S_{22L} S_{21I} S_{21A}$$

$$= R + T^2 (0.25) (0.1) (0.5)$$

$$= R + T^2 (0.0125)$$